Quantity:

The quantity is related to amount which can be measured.

Ratio:

• Definition:

Relation obtained by comparing two quantities by division is known as ratio.

If a, b and K are non zero real numbers such that a=bk then k is the ratio of a to b.

Writing manner:

The ratio of a to b written as a:b or $\frac{a}{b}$

Notes:

- 1)The term a is the first term (antecedent) and the term b is called second term (consequent)
 - 2) Second term b is always a non zero real number
 - 3) A ratio is a number. It has no unit of measurement.
 - 4) Two quantities of the ratio must be of the same kind.
 - 5) Two quantities of the ratio must be in same unit.
 - 6) Percentage is also a ratio having second term 100.

- Properties of ratio:
 - 1) The ratio remains unchanged if both the terms of the ratio are multiplied or divided by same non zero number.
 - 2) Simplest form

Since
$$\frac{a}{b} = \frac{ak}{bk}$$
 for every non zero number k

Therefore ratio $\frac{a}{b}$ and $\frac{ak}{bk}$ are the same and $\frac{a}{b}$ is its simplest form

• Order Relation (comparision)

Consider two ratios $\frac{a}{b}$ and $\frac{c}{d}$

1) If a X d > b X c then
$$\frac{a}{b} > \frac{c}{d}$$
 where b > 0, d > 0

2) If a X d < b X c then
$$\frac{a}{b} < \frac{c}{d}$$
 where b > 0, d > 0

3) If a X d = b X c then
$$\frac{a}{b} = \frac{c}{d}$$
 where b > 0, d > 0

• Properties of equal ratios

Worksheet I

Observe the following table I)

Bananas	Cost
8 (a)	16 (c)
4 (b)	8 (d)

Find
$$\frac{a}{b}$$
 and $\frac{c}{d}$

What is your conclusion? (equal ratios)

Observe the following table II)

Bananas	Cost
4 (b)	8 (d)
8 (a)	16 (c)

Find

i) $\frac{b}{a}$ and $\frac{d}{c}$ ii) $\frac{b}{a}$ and $\frac{c}{d}$

What is your conclusion? (invertendo)

III) Observe the following table

Bananas	Cost
8 (a)	4 (b)
16 (c)	8 (d)

Find

i)
$$\frac{a}{c}$$
 and $\frac{b}{d}$

i)
$$\frac{a}{c}$$
 and $\frac{b}{d}$ ii) $\frac{a}{d}$ and $\frac{b}{c}$

What is your conclusion?

(alternendo)

IV) Observe the following table

Bananas	Cost
8 + 4 (a + b)	16 + 8 (c + d)
4 (b)	8 (d)

Find i)
$$\frac{a+b}{b}$$
 and $\frac{c+d}{d}$ ii) $\frac{a+b}{c}$ and $\frac{c+d}{a}$

ii)
$$\frac{a+b}{c}$$
 and $\frac{c+d}{a}$

What is your conclusion? (componendo)

V) Observe the following table

Bananas	Cost
8 - 4 (a - b)	16 - 8 (c - d)
4 (b)	8 (d)

Find i)
$$\frac{a-b}{b}$$
 and $\frac{c-d}{d}$ ii) $\frac{a-b}{c}$ and $\frac{c-d}{a}$

ii)
$$\frac{a-b}{c}$$
 and $\frac{c-a}{a}$

What is your conclusion? (dividendo)

VI) Observe the following table

Bananas	Cost
8+4 (a+b)	16+8 (c+d)
8 - 4 (a - b)	16 - 8 (c - d)

Find
$$\frac{a+b}{a-b}$$
 and $\frac{c+d}{c-d}$

What is your conclusion?

(componendo and dividendo)