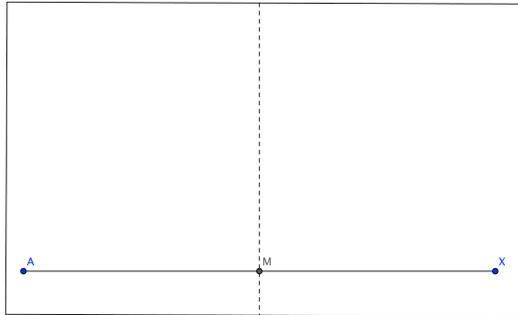


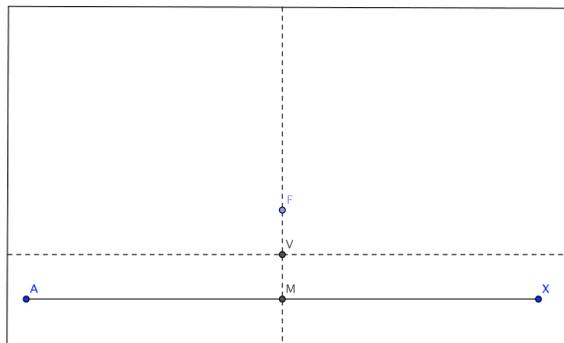
**Locus Construction (I)**

**Materials Needed:** A piece of parchment paper, pencil, ruler

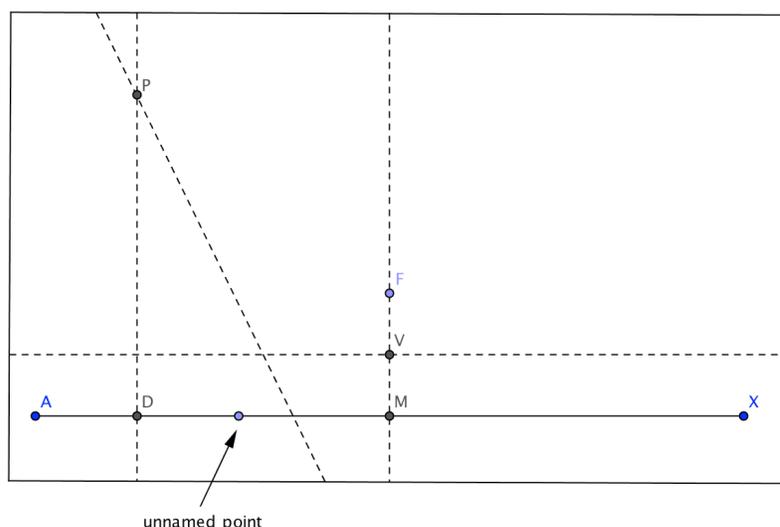
1. Use your ruler to draw a long segment that appears to be parallel to the bottom edge of your parchment paper. Place this segment at most 2 inches away from the bottom of the paper. (Don't worry if this segment isn't "perfectly parallel" to the bottom edge of the paper.)
2. Plot and label the left-most endpoint of your segment as  $A$ . Plot and label the right-most endpoint of your segment as  $X$ .
3. Fold point  $A$  on top of point  $X$ . (This will create a vertical crease that serves as the perpendicular bisector of  $\overline{AX}$ .) Label the midpoint of  $\overline{AX}$  as  $M$ . (See figure.)



4. Plot and label a point  $F$  somewhere along the vertical crease created in step (3) but less than 3 inches from  $M$ .
5. Fold point  $M$  onto point  $F$  and crease sharply creating a horizontal crease parallel to  $\overline{AX}$ . Label the intersection of this horizontal crease and the vertical crease formed in step (3) as  $V$ . (See figure.)



6. This is the most important step here, so please read carefully!
- Plot any point (leave it unnamed) on  $\overline{AX}$  that lies either to the left or right side of  $M$ . Fold point  $A$  directly on top of this point. Crease sharply. This should create a vertical crease on your paper (on the left side of  $M$ ).
  - Plot and label a point  $D$  at the intersection of  $\overline{AX}$  and vertical crease you just formed.
  - Fold point  $D$  onto point  $F$ . Crease sharply. This will create a diagonal crease somewhere on your paper.
  - Plot and label a point  $P$  at the intersection of this diagonal crease and the vertical crease formed in step (a). (See figure.)



- Take your ruler and measure the lengths  $FP$  and  $PD$  (on the left side of  $M$ .) What do you notice?
- Why is your observation in step (7) above true? What previously learned theorem justifies your observation?
- Repeat the **entire steps (6) and (7)** at least 15-25 more times. Pick the unnamed points on  $\overline{AX}$  on **both the left and right side of  $M$** . The more folds you make, the better the end product!

10. Draw a smooth curve through the set of points labeled  $P$  that you plotted by completing step (6) numerous times. If the shape of this curve looks familiar, how would you describe it?

11.

12. Now even though  $\overline{AX}$  was a segment, we could keep generating more points (all with the label  $P$ ) if our paper were large enough. So, as we complete this formal definition below, consider the segment with endpoints  $A$  and  $X$  to be a *line* instead.

After class discussion:

13. Use your observation to help complete the following definition:

**A \_\_\_\_\_ is a locus (set of points) in a plane that are  
\_\_\_\_\_ from a fixed \_\_\_\_\_,  
(called the \_\_\_\_\_) and a given line (called the \_\_\_\_\_).**